

# Naturalness of Light Neutralino Dark Matter in pMSSM after LHC, XENON100 and Planck Data

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**ABSTRACT:** We examine the possibility of a light (below 46 GeV) neutralino dark matter (DM) candidate within the 19-parameter phenomenological Minimal Supersymmetric Standard Model (pMSSM) in the light of various recent experimental results, especially from the LHC, XENON100, and Planck. We also study the extent of electroweak fine-tuning for such a light neutralino scenario in view of the null results from the searches for supersymmetry so far. Using a Markov Chain Monte Carlo likelihood analysis of the full pMSSM parameter space, we find that a neutralino DM with mass  $\gtrsim 10$  GeV can in principle still satisfy all the existing constraints. Our light neutralino solutions can be broadly divided into two regions: (i) The solutions in the 10 - 30 GeV neutralino mass range are highly fine-tuned and require the existence of light selectrons (below 100 GeV) in order to satisfy the observed DM relic density. We note that these are not yet conclusively ruled out by the existing LEP/LHC results, and a dedicated analysis valid for a non-unified gaugino mass spectrum is required to exclude this possibility. (ii) The solutions with low fine-tuning are mainly in the 30 - 46 GeV neutralino mass range. However, a major portion of it is already ruled out by the latest XENON100 upper limits on its spin-independent direct detection cross section, and the rest of the allowed points are within the XENON1T projected limit. Thus, we show that the allowed MSSM parameter space for a light neutralino DM below the LEP limit of 46 GeV, possible in supersymmetric models without gaugino mass unification, could be completely accessible in near future. This might be useful in view of the recent claims for positive hints of a DM signal in some direct detection experiments.

**KEYWORDS:** Supersymmetry, Dark Matter

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## 1 Introduction

Low-scale Supersymmetry (SUSY) (see e.g., [1, 2]) is one of the most attractive candidates for New Physics beyond the Standard Model (SM). Apart from providing successful gauge coupling unification and a solution to the gauge hierarchy problem, it offers a natural candidate for Dark Matter (DM) in our Universe in the form of the lightest supersymmetric particle (LSP). In the  $R$ -parity conserving Minimal Supersymmetric Standard Model (MSSM), the lightest neutralino ( $\tilde{\chi}_1^0$ ) is one of the most viable Weakly Interacting Massive Particle (WIMP) DM candidates (for a review, see e.g., [3, 4]). It can explain the observed DM relic density, while predicting experimentally accessible direct and indirect detection rates, over a wide range of supersymmetric model parameters, some of which are already getting constrained from the ongoing direct searches for the supersymmetric particles at the Large Hadron Collider (LHC), in combination with other low-energy data (for a review, see e.g., [5]).

The recent hints of positive signals in three DM direct detection experiments, namely, DAMA [6, 7], CoGeNT [8, 9] and CRESST-II [10], have generated a lot of interest in *light* WIMP candidates in the 5 - 50 GeV mass range. This interpretation is however challenged by the null results from various other direct detection experiments, most notably the latest XENON100 results [11], which provide the most stringent upper limits on the spin-independent WIMP-nucleon scattering cross section for  $m_\chi > 7$  GeV<sup>1</sup>. Nonetheless, due to the relatively poor sensitivity of the XENON100 experiment in the very low WIMP mass regime, it is believed that an agreement between the positive and null sets of experimental results could be possible, if at all, only in this low mass region. Hence, it might be worthwhile examining the allowed MSSM parameter space to see if there exists a *lower* bound on the lightest neutralino mass irrespective of the direct detection results.

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<sup>1</sup>More recently, the TEXONO experiment [12] has achieved slightly better sensitivity than XENON100 for  $m_\chi < 7$  GeV.

The neutralino mass eigenstates in the MSSM result from mixing of the neutral bino ( $\tilde{B}$ ), wino ( $\tilde{W}^0$ ) and higgsinos ( $\tilde{H}_d^0, \tilde{H}_u^0$ ). This mixing is determined by the MSSM  $\tan\beta$  parameter and the bino, wino and higgsino mass parameters  $M_1, M_2$  and  $\mu$ , respectively. In the SUSY models with gaugino mass unification at the Grand Unified Theory (GUT) scale, a relation between the bino and wino mass follows at the electroweak scale:  $M_1 = \frac{5}{3} \tan^2 \theta_W M_2 \approx 0.5 M_2$  (see e.g., [13]) which, after mixing, translates into a chargino-neutralino mass relation. Therefore, a lower limit on the lightest neutralino ( $\tilde{\chi}_1^0$ ) mass of about 46 GeV can be derived for these models from the Large Electron Positron (LEP) chargino mass limit [14], whereas in the constrained MSSM (cMSSM) [15] with both gaugino and sfermion mass unification, this limit increases to well above 100 GeV from the strong constraints set by the recent LHC data [5].

On the other hand, in a generic MSSM scenario without the assumption of gaugino mass unification, there is no general lower limit on the lightest neutralino mass [16]. The LEP limit on the invisible decay width of the SM  $Z$  boson applies to light neutralinos with a mass below  $m_Z/2 = 45.6$  GeV, but it depends on the  $Z\tilde{\chi}_1^0\tilde{\chi}_1^0$  coupling which could be small or even zero, depending on the higgsino component of the neutralino. In such a case, light neutralinos are mainly constrained by the DM relic density measurement as well as by the collider and flavor constraints on the SUSY parameter space. Assuming that the lightest neutralino is non-relativistic and provides the entire cold DM content of the Universe, while satisfying the LEP bounds on chargino and stau masses, Ref. [17] obtained a lower bound of  $m_{\tilde{\chi}_1^0} \gtrsim 18$  GeV. This was relaxed to about 6 GeV without violating the LEP bounds and flavor sector constraints in SUSY models with a pseudoscalar Higgs boson ( $A$ ) mass  $m_A < 200$  GeV and a large  $\tan\beta$  [18, 19]. This was even further lowered to about 3 GeV by allowing explicit  $CP$  violation in the MSSM Higgs sector [20].

Meanwhile, several new experimental results have been obtained at the LHC: (i) A new Higgs-like neutral scalar particle has been discovered [21, 22] with mass around 125 GeV which falls squarely within the MSSM-predicted range for the lightest  $CP$ -even neutral Higgs mass:  $m_h \in [115, 135]$  GeV (see e.g., [23]); (ii) The rare decay  $B_s^0 \rightarrow \mu^+\mu^-$  was observed with a branching fraction of  $\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-) = (3.2_{-1.2}^{+1.5}) \times 10^{-9}$  [24] which is in agreement with the SM expectation,  $\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-)_{\text{SM}} = (3.23 \pm 0.27) \times 10^{-9}$  [25]; (iii) The lack of a SUSY signal at the  $\sqrt{s} = 7$  and 8 TeV LHC has pushed the lower limits on the squark and gluino masses to about 1 TeV and beyond [26, 27]; (iv) Updated bounds have been obtained for the MSSM Higgs sector [28–30]. All these new results have profound implications for a light neutralino scenario within the MSSM, and some of these aspects have already been investigated in a number of recent studies [31–44]. The general conclusion is that light neutralino DM candidates with mass below about 15 GeV are severely constrained in generic MSSM scenarios (without gaugino mass unification).

Another important issue to be addressed in the light of the recent LHC results is the apparent “little hierarchy problem”, i.e., how does a multi-TeV SUSY particle spectrum conspire to give a weak-scale  $Z$ -boson mass and also a Higgs boson mass of 125 GeV? One way of analyzing this issue quantitatively is to evaluate the measure of electroweak fine-tuning (EWFT) by examining the minimization condition in the MSSM Higgs potential which determines the  $Z$ -boson mass [45, 46]. It is well-known that radiative corrections

must play a crucial role in determining the allowed SUSY parameter space necessary to generate a 125 GeV Higgs boson mass, much larger than its tree-level prediction of  $m_h \leq m_Z$ . This in general can lead to a large fine-tuning. In addition to this, the requirement of a light neutralino DM will pose a challenge for any MSSM scenario, the severity of which is however strongly model-dependent. The naturalness of various SUSY models with a neutralino LSP has been analyzed in the literature (for an incomplete list, see [41, 47–60], and references therein).

In this paper, we perform a dedicated study focusing on the naturalness of a *light* neutralino, and also examining how light the neutralino could be, after taking into account all the existing theoretical and experimental constraints. To perform such an analysis in the full 124-parameter MSSM is quite unrealistic, and hence, we need to make some well-motivated assumptions in order to reduce the number of parameters to a manageable level. Most of the earlier studies on SUSY focused on the cMSSM having only 5 parameters, assuming certain boundary conditions at the GUT-scale. However, in view of the latest null results from SUSY searches at the  $\sqrt{s} = 8$  TeV LHC, the cMSSM seems too restrictive for low-scale SUSY phenomenology as the allowed cMSSM parameter space accessible to the  $\sqrt{s} = 14$  TeV LHC is rapidly shrinking (for the latest global status, see e.g., Ref. [61–63]). Therefore, in this paper we choose not to make any assumptions at the high scale, and focus only on the low-scale MSSM parameter space from a phenomenological point of view. More precisely, we consider a  $CP$ -conserving MSSM (i.e., with no new  $CP$  phases) with Minimal Flavor Violation [64] and with first two generations of sfermions degenerate. This is widely known as the phenomenological MSSM (pMSSM) [65] (also known as ‘SUSY without prejudice’ [66]) with 19 free parameters at the electroweak scale. We also study the level of fine-tuning for the light neutralino scenario in this context.

In order to efficiently explore the 19-dimensional pMSSM parameter space, we perform a Markov Chain Monte Carlo (MCMC) likelihood analysis (for a review, see e.g., [67]), with the priors optimized for a light neutralino scenario with mass below the conservative LEP lower limit of 46 GeV. We include in our analysis the latest experimental results for SUSY searches from the LHC [26, 27] which now supersede the Tevatron results [68, 69], in addition to the existing LEP limits [14], wherever applicable. We also include the latest astrophysical/cosmological constraints for a WIMP DM from the 9-year WMAP data [70] as well as the very recently released Planck data [71]. We further examine the allowed parameter space in the light of various recent results for DM direct detection, most notably the XENON100 limits [11], as well as the indirect detection results from Fermi-LAT data [72].

We find that a light neutralino DM with mass as low as 10 GeV is still allowed in the pMSSM, while satisfying all the existing experimental constraints provided we only take the model-independent analysis results from LEP. (Including the LEP limits strictly applicable to gaugino-mass unification models allows only the solutions with  $m_{\tilde{\chi}_1^0} > 30$  GeV, in agreement with previous results [33, 34].) However, such neutralinos which are required to be mostly bino-like are severely fine-tuned and require the existence of light sleptons below 100 GeV in order to provide an efficient annihilation channel to reduce the bino relic density to be consistent with the observed limit. A dedicated analysis of

the LEP data in the context of a pMSSM scenario could eliminate this region completely. On the other hand, low fine-tuning regions can be obtained around  $m_{\tilde{\chi}_1^0} = 45$  GeV where the resonant annihilation via the  $s$ -channel  $Z$ -exchange is possible for the neutralino with a non-negligible higgsino component. However, such regions are mostly excluded by the recent XENON100 limits on the spin-independent DM-nucleon scattering cross section, and the remaining such points are well within the reach of the XENON1T [73] and LUX [74] projected limits.

Our paper is organized as follows: In Section 2, we briefly discuss the electroweak fine-tuning measure. In Section 3, we list all the pMSSM parameters and their scan ranges, and also summarize all the relevant experimental constraints used in our numerical analysis. In Section 4, we present our scan results and discuss their implications for a light neutralino DM. Finally, our conclusions are given in Section 5.

## 2 Electroweak Fine-Tuning

To quantify the amount of fine-tuning in the electroweak symmetry breaking (EWSB) sector of the MSSM, it is sufficient for us to analyze the tree-level MSSM scalar potential. Since it allows only charge-conserving vacua, we only have to minimize the scalar potential for the neutral scalar fields [1]:

$$V = (m_{H_u}^2 + \mu^2)|H_u^0|^2 + (m_{H_d}^2 + \mu^2)|H_d^0|^2 - B\mu(H_u^0 H_d^0 + \text{H.c.}) + \frac{1}{8}(g^2 + g'^2)(|H_u^0|^2 - |H_d^0|^2)^2, \quad (2.1)$$

where  $\mu$  is the SUSY-preserving bilinear Higgs superpotential parameter,  $m_{H_{u,d}}$  and  $B$  are the soft scalar masses and the bilinear coupling in the SUSY-breaking sector respectively, and  $g, g'$  the  $SU(2)_L$  and  $U(1)_Y$  gauge couplings, respectively. After minimization, we obtain the well-known relation for the  $Z$ -boson mass:

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 - m_{H_u}^2 \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2, \quad (2.2)$$

where  $\tan \beta = v_u/v_d$  is the ratio of the vacuum expectation values (vevs) of the two Higgs doublet fields  $H_u$  and  $H_d$  respectively. It is clear from Eq. (2.2) that a cancellation of the terms on the right hand side (RHS) is required in order to obtain the measured value of  $m_Z = 91.2$  GeV [5] especially if the mass parameters on the RHS are orders of magnitude larger than the weak scale which indeed seems to be the case, given the current experimental status of the direct SUSY searches [26, 27]. Thus naively speaking, the weak scale value of  $|\mu|$  can be used as a measure of fine-tuning in the MSSM.

A more sophisticated way to quantify the degree of EWFT is by using log-derivatives [46]:

$$\Delta p_i = \left| \frac{\partial \ln m_Z^2(p_i)}{\partial \ln p_i} \right| = \left| \frac{p_i}{m_Z^2} \frac{\partial m_Z^2}{\partial p_i} \right|, \quad (2.3)$$

where  $p_i$ 's are the parameters that determine the observable  $Z$ -mass at tree-level. From Eq. (2.2), we have  $p_i = \{\mu^2, b, m_{H_u}, m_{H_d}\}$  (with  $b \equiv B\mu$ ), and the total measure of the

EWFT is defined as

$$\Delta_{\text{tot}} = \sqrt{(\Delta\mu^2)^2 + (\Delta b)^2 + (\Delta m_{H_u}^2)^2 + (\Delta m_{H_d}^2)^2}, \quad (2.4)$$

with the individual  $\Delta p_i$ 's given by [75]

$$\begin{aligned} \Delta\mu^2 &= \frac{4\mu^2}{m_Z^2} \left( 1 + \frac{m_A^2 + m_Z^2}{m_A^2} \tan^2 2\beta \right), \\ \Delta b &= \left( 1 + \frac{m_A^2}{m_Z^2} \right) \tan^2 2\beta, \\ \Delta m_{H_u}^2 &= \left| \frac{1}{2} \cos 2\beta + \frac{m_A^2}{m_Z^2} \cos^2 \beta - \frac{\mu^2}{m_Z^2} \right| \left( 1 - \frac{1}{\cos 2\beta} + \frac{m_A^2 + m_Z^2}{m_A^2} \tan^2 2\beta \right), \\ \Delta m_{H_d}^2 &= \left| -\frac{1}{2} \cos 2\beta + \frac{m_A^2}{m_Z^2} \sin^2 \beta - \frac{\mu^2}{m_Z^2} \right| \left( 1 + \frac{1}{\cos 2\beta} + \frac{m_A^2 + m_Z^2}{m_A^2} \tan^2 2\beta \right). \end{aligned} \quad (2.5)$$

Here  $m_A^2 = B\mu(\tan\beta + \cot\beta)$  is the MSSM pseudo-scalar Higgs mass, and we have assumed  $\tan\beta > 0$ . Values of  $\Delta_{\text{tot}} \gg 1$  indicate significant fine-tuning. Note that in the limit of large  $\tan\beta$ , the quantities  $\Delta m_{H_u}^2$  and  $\Delta m_{H_d}^2$  in Eq. (2.5) are small, and

$$\Delta\mu^2 \simeq \frac{4\mu^2}{m_Z^2}, \quad \Delta b \simeq \frac{4m_A^2}{m_Z^2 \tan\beta}. \quad (2.6)$$

Thus in the limit of large  $\tan\beta$ , we recover the naive result that fine-tuning increases with increasing  $|\mu|$ .

We should note here that including loop corrections to Eq. (2.2), one finds the largest contribution to be coming from the (s)top loop which feeds into the soft mass of the Higgs [13]:

$$\delta m_{H_u}^2 = -\frac{3y_t^2}{8\pi^2} (m_{\tilde{t}_L}^2 + m_{\tilde{t}_R}^2 + |A_t|^2) \log \left( \frac{\Lambda}{m_{\tilde{t}}} \right), \quad (2.7)$$

where  $y_t$  is the top-quark Yukawa coupling,  $A_t$  is the third-generation  $A$ -term in the SUSY-breaking sector, and  $\Lambda$  is some high scale where the stop masses  $m_{\tilde{t}_{L,R}}$  are generated from the SUSY-breaking mechanism. Even for a low-scale SUSY-breaking scenario (such as gauge mediation), this requires a fine-tuning of at least a few percent in order to get the observed  $Z$ -mass and it becomes worse for heavy stop masses [76]. A heavy physical stop mass  $m_{\tilde{t}} \gtrsim 500$  GeV is anyway required to provide large enough radiative corrections to the light  $CP$ -even Higgs mass to raise it to the vicinity of 125 GeV from its tree-level value  $\leq m_Z$  [13]:

$$\delta m_{h^0}^2 = \frac{3m_t^4}{16\pi^2 v^2} \left[ \log \left( \frac{m_{\tilde{t}_L}^2 m_{\tilde{t}_R}^2}{m_t^4} \right) + \frac{X_t^2}{m_{\tilde{t}_L} m_{\tilde{t}_R}} \left( 1 - \frac{X_t^2}{12m_{\tilde{t}_L} m_{\tilde{t}_R}} \right) \right], \quad (2.8)$$

where  $X_t = A_t - \mu \cot\beta$  is the stop mixing parameter. A fine-tuning measure  $\Delta_{m_h}$  for the Higgs mass can be defined analogous to Eq. (2.3), and for a particular choice of some of the SUSY parameters, it was found that  $\Delta_{m_h} > 75$  (100) in order to achieve a Higgs mass of

124 (126) GeV and the corresponding stop mass is always heavier than 300 (500) GeV [77]. The fine-tuning due to Eqs. (2.7) and (2.8) could in principle be added in quadratures to our “total” fine-tuning parameter defined by Eq. (2.4), but since their specific values are scale-dependent <sup>2</sup> and adds to some arbitrariness in its definition, we do not include them in our analysis.

### 3 Parameters and Constraints

We consider the pMSSM with 19 free parameters at the SUSY scale, as shown in Table 1. We further assume that the lightest neutralino is the LSP, and our goal is to examine how light and natural the neutralino could be while satisfying all the existing theoretical and experimental constraints on the MSSM parameter space. In particular, we focus on the lightest neutralino masses below the LEP limit of 46 GeV [14] which is strictly valid assuming gaugino mass unification at the GUT-scale. We perform a numerical scan over the 19-dimensional pMSSM parameter space using a MCMC-based likelihood analysis optimized for such light neutralino scenarios with the prior ranges given in Table 1. These

Parameter	Description	Prior Range
$\tan \beta$	Ratio of the scalar doublet vevs	[1, 60]
$\mu$	Higgs-Higgsino mass parameter	[−3, 3] TeV
$M_A$	Pseudo-scalar Higgs mass	[0.3, 3] TeV
$M_1$	Bino mass	[−0.5, 0.5] TeV
$M_2$	Wino mass	[−1, 1] TeV
$M_3$	Gluino mass	[0.8, 3] TeV
$m_{\tilde{q}_L}$	First/second generation $Q_L$ squark	[0, 3] TeV
$m_{\tilde{u}_R}$	First/second generation $U_R$ squark	[0, 3] TeV
$m_{\tilde{d}_R}$	First/second generation $D_R$ squark	[0, 3] TeV
$m_{\tilde{\ell}_L}$	First/second generation $L_L$ slepton	[0, 3] TeV
$m_{\tilde{e}_R}$	First/second generation $E_R$ slepton	[0, 3] TeV
$m_{\tilde{Q}_{3L}}$	Third generation $Q_L$ squark	[0, 3] TeV
$m_{\tilde{t}_R}$	Third generation $U_R$ squark	[0, 3] TeV
$m_{\tilde{b}_R}$	Third generation $D_R$ squark	[0, 3] TeV
$m_{\tilde{L}_{3L}}$	Third generation $L_L$ slepton	[0, 3] TeV
$m_{\tilde{\tau}_R}$	Third generation $E_R$ slepton	[0, 3] TeV
$A_t$	Trilinear coupling for top quark	[−10, 10] TeV
$A_b$	Trilinear coupling for bottom quark	[−10, 10] TeV
$A_\tau$	Trilinear coupling for $\tau$ -lepton	[−10, 10] TeV

**Table 1.** The pMSSM parameters and their range of values used in our numerical analysis.

particular ranges are chosen in order to economize the scan time and to focus only on the

<sup>2</sup>The SUSY-scale by convention is usually taken to be the geometric mean of the two stop masses.



SUSY parameter space not yet disfavored by the combined direct search results from the LEP [14], Tevatron [68, 69] and LHC [26, 27], as discussed later in this section. For the SM parameters  $\alpha_s(m_Z)$ ,  $\alpha_{\text{em}}(m_Z)$ ,  $m_W$ ,  $m_t$  and  $m_b$ , we use the standard values as given in Ref. [5].

Apart from the direct collider constraints on the sparticle masses, there exist various theoretical and experimental constraints which must be imposed on the pMSSM parameter space in our analysis. As a standard theoretical requirement, our sparticle spectrum for each allowed point in the parameter space must be tachyon-free and should not lead to color- and charge-breaking minima in the scalar potential [78]. We also require that the scalar potential is bounded from below and is consistent with electroweak symmetry breaking. From the radiative electroweak symmetry breaking arguments, we can restrict the  $\tan\beta$  parameter to be roughly between 1 - 60, as given in Table 1.

The various experimental constraints from direct collider searches, Higgs and flavor sectors, and astrophysical/cosmological data used in our analysis are summarized below.

### Invisible $Z$ -decay Width

The precise measurement of the  $Z$ -boson decay width at LEP:  $\Gamma_Z^{\text{tot}} = 2495.2 \pm 2.3$  MeV [79] puts severe constraints on light neutralinos and charginos with mass  $< m_Z/2$ . From the LEP measurements of the invisible decay width of the  $Z$ -boson:  $\Gamma_Z^{\text{inv}} = (499.0 \pm 1.5)$  MeV [79], the parameter space for the lightest neutralino in our case is restricted to mostly gaugino-like scenarios ( $|\mu| \gg M_{1,2}$ ) since the neutralino coupling to  $Z$  is only via its higgsino component. The allowed fraction of the higgsino component for a given neutralino mass can be calculated using the following expression for the partial decay width of the  $Z$ -boson to neutralinos [80]:

$$\frac{\Gamma(Z \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0)}{\Gamma(Z \rightarrow \nu \bar{\nu})} = 2 \left( 1 - \frac{4m_{\tilde{\chi}_1^0}^2}{m_Z^2} \right)^{1/2} \left[ \left( 1 - \frac{m_{\tilde{\chi}_1^0}^2}{m_Z^2} \right) [(O_{11}^L)^2 + (O_{11}^R)^2] + \frac{6m_{\tilde{\chi}_1^0}^2}{m_Z^2} O_{11}^L O_{11}^R \right] \quad (3.1)$$

where  $\Gamma(Z \rightarrow \nu \bar{\nu}) = (501.62 \pm 0.10)$  MeV is the SM contribution to its invisible decay width (for 3 neutrino species). The components  $O_{ij}^{L,R}$  are defined as

$$O_{ij}^L = -\frac{1}{2} N_{i3} N_{j3}^* + \frac{1}{2} N_{i4} N_{j4}^*, \quad O_{ij}^R = -(O_{ij}^L)^* \quad (3.2)$$

with  $N_{ij}$  measuring the gaugino-Higgsino mixing:

$$\tilde{\chi}_i^0 = \sum_{k=1}^4 N_{ik} \tilde{\psi}_k^0, \quad \text{where } \tilde{\psi}^0 = (\tilde{B}, \tilde{W}^0, \tilde{H}_u^0, \tilde{H}_d^0). \quad (3.3)$$

Using the LEP measurement of the invisible  $Z$ -decay width, the following constraint can be derived:

$$\Gamma(Z \rightarrow \tilde{\chi}_i^0 \tilde{\chi}_j^0) < 3 \text{ MeV} \quad \text{if } (m_{\tilde{\chi}_i} + m_{\tilde{\chi}_j}) < m_Z \quad (3.4)$$

Note that this constraint should apply to *all* light neutralinos satisfying this condition, not just the LSP ( $i = j = 1$  in Eq. 3.4). However, it is unlikely that decays such as



$Z \rightarrow \tilde{\chi}_2^0 \tilde{\chi}_1^0$  will be kinematically allowed, and in such cases,  $\tilde{\chi}_2^0$  will mostly decay to visible final states. Similarly, the decays  $Z \rightarrow \tilde{\nu}_i \tilde{\nu}_j$  are not kinematically allowed for the parameter space examined here, and hence, they do not contribute to the purely invisible width of the  $Z$ -boson.

### Exclusion Limits from Collider Searches

The experimental lower limits on the sparticle masses are usually quoted assuming gaugino and/or sfermion mass universality at the GUT scale. In a generic MSSM setup, most of these constraints can be relaxed, or even circumvented, for example in case of small mass splitting with the LSP or in case of small couplings to the SM vector bosons. Since we are interested in light neutralino LSPs here, we must carefully interpret the direct search limits in order to be able to include all the allowed pMSSM parameter space.

**Neutralino:** As already mentioned in Section 1, there are no rigorous lower limits on the neutralino masses in the MSSM from direct collider searches. The LEP limits [14, 81]

$$m_{\tilde{\chi}_1^0} > 46 \text{ GeV}, m_{\tilde{\chi}_2^0} > 62.4 \text{ GeV}, m_{\tilde{\chi}_3^0} > 99.9 \text{ GeV}, m_{\tilde{\chi}_4^0} > 116.0 \text{ GeV} \quad (3.5)$$

were derived assuming gaugino mass unification at the GUT scale, and hence, relating the neutralino mass to the chargino mass. Moreover, for a (mostly) bino-like neutralino, which is required to be the case for  $m_{\tilde{\chi}_1^0} < m_Z/2$  in order to avoid the  $Z$ -width constraint, its production via  $s$ -channel exchange of  $Z/\gamma^*$  is (negligible) absent. The  $t$ -channel production cross-section via selectron exchange is also expected to be small for selectron masses above the LEP limit (see below). Thus, we can easily satisfy the LEP upper limits on the neutralino pair-production cross sections  $\sigma(e^+e^- \rightarrow \tilde{\chi}_i^0 \tilde{\chi}_j^0)$  [81, 82] for a mostly bino-like neutralino LSP. Similarly, the Tevatron [83] and LHC [84] SUSY searches for final states involving  $Z$ -bosons cannot constrain a bino-like neutralino.

**Chargino:** Charginos can be pair-produced at LEP via  $s$ -channel exchange of  $Z/\gamma^*$  or  $t$ -channel exchange of electron-sneutrino, with destructive interference. It dominantly decays to  $\ell \tilde{\nu}$ , if kinematically allowed. If not, the three-body decay to  $f \bar{f}' \tilde{\chi}_i^0$  via virtual  $W$ -boson or sfermions becomes important in which case, the final state fermions ( $f, \bar{f}'$ ) are dominantly leptonic (hadronic) if the sleptons are light (heavy). From the combined searches in fully-hadronic, semi-leptonic and fully-leptonic decay modes, LEP has derived a general lower limit of 103.5 GeV [14] which is valid for pMSSM as well, except in corners of phase space where (i) the detection efficiencies are reduced, e.g., when the mass differences  $\Delta m_+ = m_{\tilde{\chi}_1^\pm} - m_{\tilde{\chi}_1^0}$  or  $\Delta m_\nu = m_{\tilde{\chi}_1^\pm} - m_{\tilde{\nu}}$  are very small (below a few GeV); or (ii) the chargino production cross section is suppressed, e.g., when the electron sneutrino mass is small, thus leading to a destructive interference between  $s$ - and  $t$ -channel Feynman diagrams. Dedicated searches for such scenarios have also been performed. For instance, for small  $\Delta m_+ < 3 \text{ GeV}$  but with large sneutrino mass, the limit becomes  $m_{\tilde{\chi}_1^\pm} > 91.9 \text{ GeV}$  for degeneracy in the gaugino region ( $|M_1| \sim |M_2| \ll |\mu|$ ) while  $m_{\tilde{\chi}_1^\pm} > 92.4 \text{ GeV}$  for degeneracy in the higgsino region ( $|\mu| \ll |M_1|, |M_2|$ ) [14]. Without assuming gaugino mass unification, a lower limit of  $m_{\tilde{\chi}_1^\pm} > 70 \text{ GeV}$  was set for any  $\Delta m_+$  and  $m_{\tilde{\nu}} > 300 \text{ GeV}$ . For smaller sneutrino masses, the sensitivity decreases due to the reduced pair production cross

section and also due to reduced selection efficiency. In such situations where none of the above mass limits can apply, the generic lower limit of approximately 45 GeV, derived from the analysis of the  $Z$ -width, is still valid since this is independent of the field composition and of the decay modes of the charginos. Note that unlike neutralinos which couple to the  $Z$ -boson only via their higgsino component, the charginos couple to  $Z$  via both their gaugino as well as higgsino components; so it is not possible to avoid the  $Z$ -width constraint for a light chargino.

**Sneutrino:** Light sneutrinos can only decay invisibly to  $\nu\tilde{\chi}_1^0$  unless the decays to charginos and heavier neutralinos are not kinematically suppressed. The invisible width of the  $Z$ -boson puts a lower limit on the left-sneutrino mass of 43.7 GeV, which improves slightly to 44.7 GeV if all three sneutrinos are mass-degenerate. Note that the lightest left-sneutrino by itself cannot be a cold DM candidate [85, 86], and we must introduce a mixing with a SM singlet sneutrino to make it a viable DM candidate (see, e.g., [87–93]). Since we are dealing here only with the MSSM field content and do not have a right-sneutrino component, we discard those points for which the sneutrino is the LSP.

**Slepton:** Studies of the  $Z$ -boson width and decays put a lower bound on the slepton masses  $m_{\tilde{\ell}_{R(L)}} > 40$  (41) GeV, independently of the decay modes for individual sleptons ( $\tilde{\ell} = \tilde{e}, \tilde{\mu}, \tilde{\tau}$ ). This limit improves to 43 GeV if all the three slepton flavors are mass-degenerate. Tighter limits can be obtained assuming that sleptons are pair-produced at LEP, and each slepton dominantly decays to  $\ell\tilde{\chi}_1^0$ , thus leading to two back-to-back leptons and missing transverse momentum. These limits are valid for a mass splitting  $\Delta m_\ell = m_{\tilde{\ell}} - m_{\tilde{\chi}_1^0} > 15$  GeV so that the final state leptons are not too soft. Moreover, the LEP results are interpreted assuming that only  $\tilde{\ell}_R\tilde{\ell}_R$  production contributes, and hence, the limits are usually quoted for  $\tilde{\ell}_R$ , since it is typically lighter than  $\tilde{\ell}_L$  in most SUSY models, and has a weaker coupling to the  $Z$ -boson so that the limits are more conservative. This is a good approximation for selectrons and smuons, but not for staus which can have significant mixing between the flavor eigenstates  $\tilde{\tau}_L$  and  $\tilde{\tau}_R$ . The most conservative limit on the mass of the lightest stau is obtained with a mixing angle  $\theta_{\tilde{\tau}} \simeq 52^\circ$  which minimizes the production cross section.

The slepton mass limits of  $\mathcal{O}(100)$  GeV quoted in Ref. [14] were derived under the assumption of gaugino mass unification at the GUT scale which was used to fix the masses and composition of neutralinos. It was also assumed that the slepton branching ratio to  $\ell\tilde{\chi}_1^0$  is nearly 100% which is a good approximation if the second lightest neutralino is heavy enough to suppress the cascade decay into  $\ell\tilde{\chi}_2^0$  followed by  $\tilde{\chi}_2^0 \rightarrow f\bar{f}\tilde{\chi}_1^0$  or  $\tilde{\chi}_1^0\gamma$ . For smuons and staus, the LEP limits are independent of the MSSM parameters [94], and hence, directly applicable to our case. However, the selectron mass limit will be different if we do not assume gaugino mass unification due to a different production cross section involving the  $t$ -channel neutralino exchange, in addition to the usual  $s$ -channel  $\gamma^*/Z$  exchange. Since there is no dedicated analysis of the LEP data addressing this issue available in the literature and this is beyond the scope of our present work, we only use the generic lower bound for  $\tilde{e}$  derived from the  $Z$ -width in our numerical analysis, but will also comment on the implications of the tighter selectron mass bound from LEP on our

light neutralino scenario. We will also include the latest 95% C.L. LHC exclusion limits for slepton pair production interpreted in the slepton-neutralino mass plane of pMSSM [95] which are applicable to both left- and right-handed selectrons and smuons.

**Gluino and Squarks:** The current LEP limits on the squark masses are similar to the slepton mass limits of  $\mathcal{O}(100)$  GeV. However, since squarks are colored objects, their production cross sections are much higher at hadron colliders. The highest sensitivity on squark and gluino production now comes from the LHC experiments. The generic lower limit on the first/second generation squark masses is 600 - 750 GeV and on the gluino mass is 700 - 900 GeV, as set for simplified SUSY models by the ATLAS analysis of the 8 TeV LHC data [26]. The corresponding CMS limits are very similar [27]. However, from the latest global fit of pMSSM after the LHC results [59] (see also Ref. [96, 97] for an earlier global fit of pMSSM), the corresponding lower limit on squark mass is  $m_{\tilde{q}} \gtrsim 500$  GeV, and hence, we use this value to constrain our pMSSM parameter space.

The LHC and Tevatron limits on the third generation squarks are usually weaker since the amount of bottom and top quark content in the proton is negligible, and hence, the direct production of bottom and top squark is suppressed with respect to the first/second generation squarks. The current exclusion limit for top squarks is between 300 - 600 GeV from the LHC data, depending on the decay channel [26, 27]. Similar limits have been derived for the bottom squark as well. Following the latest global fit of pMSSM [59], we set the lower limits for light top squark and sbottom masses at 400 GeV and 300 GeV, respectively. Note that these limits are applicable as long as the light stop/sbottom is not highly mass degenerate with the lightest neutralino (with  $\Delta m < 10$  GeV or so) which always turns out to be the case for our light neutralino solutions satisfying all the other constraints. Thus we do not have any light sbottom solutions as considered in Ref. [38].

The lower limits on the sparticle masses derived from the above discussion are summarized in Table 2. We emphasize here that for a light neutralino DM with  $m_{\tilde{\chi}_1^0} < m_Z/2$  as considered in our case, the dominant annihilation channels will be the  $t$ -channel processes mediated by light sfermions. The neutralino/chargino co-annihilation is also important if  $\Delta m_+$  is small. Hence, the lower limits on the chargino and sfermion masses as given in Table 2 are crucial ingredients in our numerical analysis.

### $B_s \rightarrow \mu^+ \mu^-$

The rare decay  $B_s \rightarrow \mu^+ \mu^-$  is known to be a sensitive channel for new physics since its SM predicted rate is small due to helicity suppression. Recently, the first evidence for this decay was observed by the LHCb collaboration with the measured branching ratio:  $\mathcal{B}(B_s \rightarrow \mu^+ \mu^-) = (3.2_{-1.2}^{+1.5}) \times 10^{-9}$  [24] which is in excellent agreement with the SM prediction of  $(3.23 \pm 0.27) \times 10^{-9}$  [25], thus raising some concerns for the “health” of SUSY. However, it must be noted that the upper limit derived from the latest LHCb result is actually slightly *weaker* than the earlier upper limit of  $< 4.5 \times 10^{-9}$  [98]. The effect of the new results is mostly felt in the large  $\tan \beta > 50$  regions of the MSSM parameter space [99] which are also strongly constrained from direct SUSY searches and the MSSM Higgs searches.

Particle	Mass limit (GeV)	Validity Condition
$\tilde{\chi}_1^\pm$	103.5	$m_{\tilde{\chi}_1^+} - m_{\tilde{\chi}_1^0} > 3 \text{ GeV}, m_{\tilde{f}} > m_{\tilde{\chi}^\pm}$
	70	$m_{\tilde{\nu}} > 300 \text{ GeV},  \mu  \geq  M_2 $
	45	generic LEP bound
$\tilde{\mu}_R$	88	$m_{\tilde{\mu}_R} - m_{\tilde{\chi}_1^0} > 15 \text{ GeV}, \text{BR}(\tilde{\mu} \rightarrow \mu \tilde{\chi}_1^0) = 1$
$\tilde{\tau}_1$	76	$m_{\tilde{\tau}_1} - m_{\tilde{\chi}_1^0} > 15 \text{ GeV}, \text{BR}(\tilde{\tau} \rightarrow \tau \tilde{\chi}_1^0) = 1$
$\tilde{e}_R$	95	$m_{\tilde{e}_R} - m_{\tilde{\chi}_1^0} > 15 \text{ GeV}, \text{BR}(\tilde{e} \rightarrow e \tilde{\chi}_1^0) = 1,$ $\mu = -200 \text{ GeV}, \tan \beta = 2$
$\tilde{\ell}_R (L)$	40 (41)	generic LEP bound
$\tilde{\nu}$	43.7	generic LEP bound
$\tilde{g}$	800	
$\tilde{q}$	500	
$\tilde{t}_1$	400	
$\tilde{b}_1$	300	

**Table 2.** The lower limits on the sparticle masses used in our numerical analysis. The chargino and slepton mass limits are derived from the LEP data [14] while the squark and gluino mass limits are derived from the LHC data [26, 27] which now supersede the LEP as well as the Tevatron [68, 69] limits.

### $b \rightarrow s\gamma$

We have also included the constraint from the radiative  $B$ -meson decay branching ratio,  $\mathcal{B}(b \rightarrow s\gamma) = (3.55 \pm 0.24 \pm 0.09) \times 10^{-4}$  [100] which is somewhat higher than the SM prediction of  $(3.15 \pm 0.23) \times 10^{-4}$  [101]. Thus large SUSY corrections are preferred which mainly occur for light chargino and top squarks and for large  $\tan \beta$  [102].

### $(g - 2)_\mu$

Another important constraint comes from the muon anomalous magnetic moment  $a_\mu \equiv (g - 2)_\mu/2$  which gives a more than  $3\sigma$  discrepancy with the SM prediction:  $\delta a_\mu = (26.1 \pm 8.0) \times 10^{-10}$  [103]. The SUSY contribution to  $\delta a_\mu$  can explain this discrepancy with relatively light smuons and/or large  $\tan \beta$  [104–106], and  $\mu < 0$  region of the SUSY parameter space is strongly disfavored (unless the electroweak gaugino masses  $M_1, M_2 < 0$ ).

### Higgs Sector

For the light  $CP$ -even Higgs mass, we have chosen the value of  $m_h = (125 \pm 2) \text{ GeV}$ , following the latest best-fit mass measurements of the Higgs-like particle discovered at the LHC:  $(125.2 \pm 0.3 \pm 0.6) \text{ GeV}$  (ATLAS) [107] and  $(125.8 \pm 0.4 \pm 0.4) \text{ GeV}$  (CMS) [108]. For the other MSSM Higgs bosons, we ensure that all our allowed points satisfy the latest LHC constraints on the  $m_A - \tan \beta$  plane [109, 110] and on the MSSM charged Higgs mass [111, 112] which are related to each other at tree-level by  $m_{H^\pm}^2 = m_A^2 + m_W^2$ . Note that the non-decoupling region with light  $m_A \sim 95 - 130 \text{ GeV}$ , almost mass-degenerate with the

light  $CP$ -even Higgs, and with the heavy  $CP$ -even Higgs SM-like, is disfavored [113, 114] by the latest LHC Higgs data and flavor constraints, especially the  $B_s \rightarrow \mu^+ \mu^-$  and  $b \rightarrow s \gamma$ . Hence, we work in the decoupling region with  $m_A > 300$  GeV with the light  $CP$ -even Higgs SM-like with mass in the vicinity of 125 GeV, and with the heavy  $CP$ -even Higgs nearly mass-degenerate with the  $CP$ -odd Higgs. Also note that for a mostly bino-like neutralino, the  $h\tilde{\chi}_1^0\tilde{\chi}_1^0$  coupling is small enough to satisfy the current global limit on the Higgs invisible decay branching ratio:  $\text{BR}_{\text{inv}} < 0.28$  at 95% CL [115].

### Dark Matter Constraints

The latest results from Planck give the current relic density of the cold dark matter content in our universe to be  $\Omega_\chi h^2 = 0.1199 \pm 0.0027$  at 68% CL [71]. The corresponding value from the 9-year WMAP data is  $\Omega_\chi h^2 = 0.1148 \pm 0.0019$  [70]. For the relic density of the neutralino DM in our case, we only require it to satisfy the WMAP  $2\sigma$  upper bound combined with 10% theoretical uncertainty:  $\Omega_{\tilde{\chi}_1^0} h^2 < 0.138$  which also encompasses the latest observed value from Planck. The cases where the neutralino relic density is below the corresponding WMAP lower bound,  $\Omega_{\tilde{\chi}_1^0} h^2 < 0.091$ , could correspond to some multi-component DM scenario (see e.g., [116–125]).

As far as the DM direct detection constraints are concerned, since there is no unanimous upper bound on the direct detection cross section, we do not put this constraint a priori on the model parameter space. However, as we will see later, most of the allowed parameter space satisfying the other constraints also satisfy the most stringent upper limit on the spin-independent DM-nucleon scattering cross section set by the XENON100 experiment [11]. Note that for  $m_\chi > 10$  GeV, the spin-independent direct detection constraints are more stringent than the collider constraints from monojet [126, 127] and isolated monophoton CMS-monoph, ATLAS-monoph searches at the LHC as well as from the LEP mono-photon data [130].

Complementary to the direct detection constraints, there exist indirect detection constraints which are mostly sensitive to light WIMPs annihilating to SM fermions which eventually lead to gamma-ray signals. A lower limit of  $m_{\tilde{\chi}_1^0} \gtrsim 10$  GeV was derived from the CMB constraints [131–135]<sup>3</sup>, assuming a velocity-independent annihilation cross section of  $\langle \sigma_a v \rangle = 3 \times 10^{-26} \text{cm}^3 \cdot \text{s}^{-1}$ . Under the same assumption, the Fermi-LAT data put lower bounds of  $m_{\tilde{\chi}_1^0} \gtrsim 27$  GeV for annihilation to  $b\bar{b}$  channel and  $m_{\tilde{\chi}_1^0} \gtrsim 37$  GeV for  $\tau^+ \tau^-$  channel [137]. However, these bounds can be relaxed if we include the velocity-dependent contributions, as shown for pMSSM in Ref. [138]. In our numerical analysis, we include the latest Fermi-LAT 95% CL upper limit on the integrated  $\gamma$ -ray flux:  $\phi_\gamma < 4 \times 10^{-10} \text{cm}^{-2} \cdot \text{s}^{-1}$  [72].

The various experimental constraints discussed above and used in our numerical analysis, in addition to the sparticle mass limits listed in Table 2, are summarized in Table 3.

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<sup>3</sup>Similar limits have also been derived from BBN constraints [136].

Parameter	Constraint
$m_h$	$(125 \pm 2) \text{ GeV}$
$\Gamma_Z^{\text{invisible}}$	$< 3 \text{ MeV}$
$\Omega_{\tilde{\chi}_1^0} h^2$	$< 0.138$
$\phi_\gamma$	$< 4 \times 10^{-10} \text{ cm}^{-2} \cdot \text{s}^{-1}$
$\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)$	$(3.2_{-1.2}^{+1.5}) \times 10^{-9}$
$\mathcal{B}(b \rightarrow s \gamma)$	$(3.55 \pm 0.26) \times 10^{-4}$
$\delta a_\mu$	$(26.1 \pm 8.0) \times 10^{-10}$

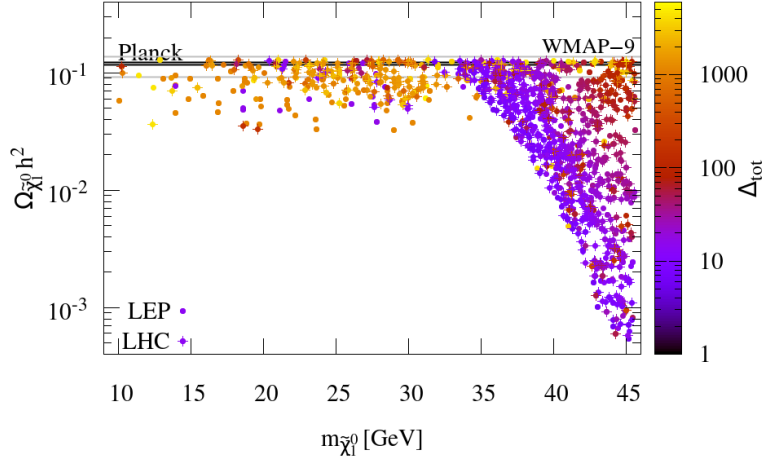
**Table 3.** The relevant experimental constraints used in our analysis, in addition to those listed in Table 2.

## 4 Results

In order to scan the 19-dimensional pMSSM parameter space more efficiently while satisfying all the constraints listed in Tables 2 and 3, we have performed a MCMC analysis using a Gaussian distribution of likelihood function:  $f(x, x_0, \sigma) = \exp[-(x - x_0)^2/2\sigma^2]$  for all the observables, with a preferred value  $x_0 \pm \sigma$ . We have used `Cac1HEP2.3` [139] and `micrOMEGAs2.4` [140–142] to compute all the observables, together with `SoftSUSY` [143] for calculating the particle spectrum.

First we discuss our MCMC scan results for the relic density of a light neutralino DM candidate as shown in Figure 1. We require all the allowed points (shown as circles) to satisfy the experimental constraints given in Table 3, along with the LEP limits on sparticle masses given in Table 2. The latest LHC results put much tighter bounds on the strongly interacting squarks and gluinos and further eliminate some of these otherwise allowed parameter space, as shown by the starred points in Figure 1. The WMAP-9  $2\sigma$  band is shown in grey, whereas the latest Planck result is shown as dark shaded region. We find that light neutralinos with mass as low as 10 GeV are still allowed, though severely fine-tuned with the electroweak fine-tuning measure defined by Eq. (2.4):  $\Delta_{\text{tot}} \gg 1$ . This can be understood as follows by analyzing the gaugino and higgsino components of the lightest neutralino as well as its dominant annihilation channels.

The bino, wino and higgsino fractions of the lightest neutralino for all the allowed points in our pMSSM parameter space are shown in Figure 2. We reproduce the well-known result that the lightest neutralino is mostly bino-like for masses below  $m_Z/2$ , mainly due to the invisible  $Z$ -decay width constraint in Eq. (3.4). However, a purely bino DM tends to overclose the universe since its annihilation cross section is  $p$ -wave suppressed and is typically much smaller than the required thermal WIMP annihilation rate of  $3 \times 10^{-26} \text{ cm}^3 \cdot \text{s}^{-1}$ . One alternative is to consider a “well-tempered” neutralino [144] which corresponds to the boundary between a pure bino and a pure higgsino or wino. Another possibility to reduce the bino relic density is by annihilation via the  $t$ -channel slepton exchange (the so-called “bulk region”) which is efficient for light sleptons, or by using co-annihilation with a light stau, stop, sbottom, chargino or second-lightest neutralino. We



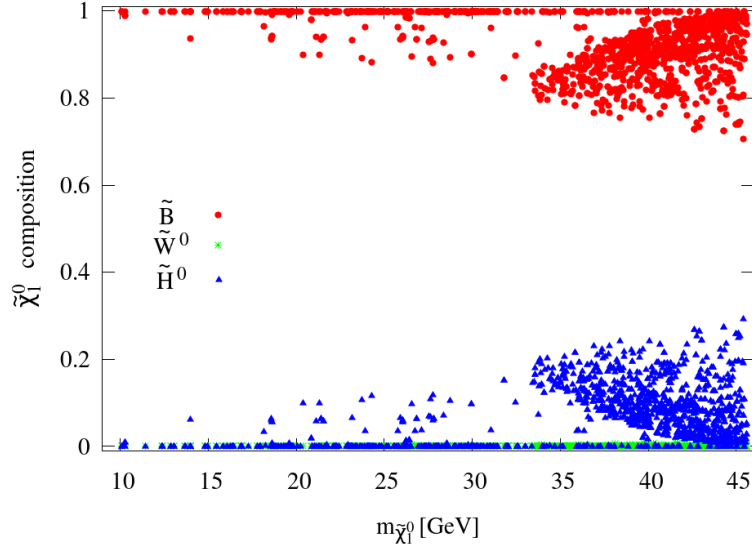
**Figure 1.** The relic density of a light neutralino DM in pMSSM satisfying all the experimental constraints discussed in Section 3. The color-coding denotes the fine-tuning measure defined by Eq. (2.4). The points denoted by circles satisfy all the experimental constraints, except that the squark masses are only required to satisfy the LEP lower limits. For the starred points (a subset of the circled points), the corresponding squark masses satisfy the latest LHC constraints. The top (bottom) grey horizontal line shows the  $2\sigma$  upper (lower) limit of the cold dark matter relic density from WMAP-9 data, whereas the black (shaded) region shows the  $1\sigma$  allowed range from the recent Planck data.

find that most of the points with  $m_{\tilde{\chi}_1^0}$  close to 45 GeV can have a non-negligible higgsino component, and hence, can easily satisfy the WMAP upper limit on the relic density since there is a resonant annihilation via  $Z$ -mediated  $s$ -channel. These points are also less fine-tuned. On the other hand, the light neutralino DM points in the 10 - 30 GeV range as shown in Figure 1 have to be mostly bino-like and lie either in the bulk or co-annihilation region, thus leading to significant fine-tuning.

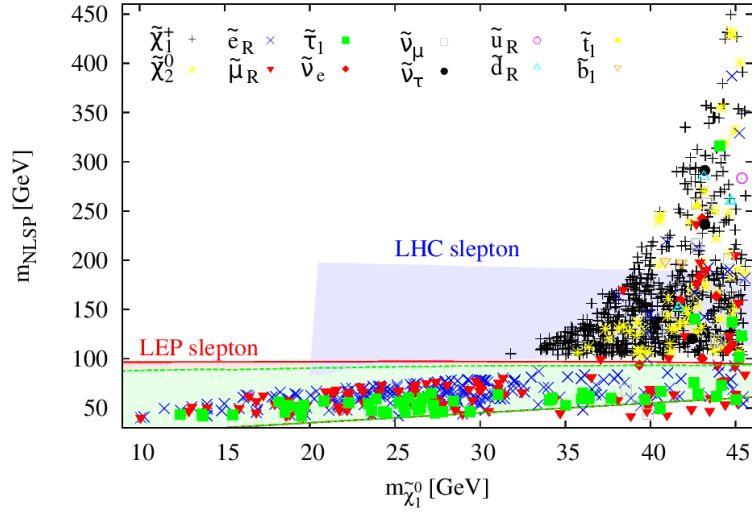
This is further clarified in Figure 3 where we show the various next-to-lightest supersymmetric particles (NLSPs) and their masses as a function of the lightest neutralino mass. We see that all the allowed points with  $m_{\tilde{\chi}_1^0} < 30$  GeV have a charged slepton NLSP with mass below 100 GeV. Especially the points with a light stau are severely fine-tuned since they usually require a mass suppression by the off-diagonal elements in the slepton mass matrix, or a large  $\mu$ -term. We also show in Figure 3 the LEP exclusion regions in the charged slepton-neutralino mass plane, derived under the assumption of gaugino mass unification [14]. The limits for light smuons and staus are still applicable to the pMSSM case as long as  $\Delta m_\ell > 15$  GeV, but not directly to light selectrons if we assume non-universal gaugino masses, and hence, can still allow the low neutralino mass regime. The latest 95% C.L. ATLAS exclusion limits [95] are also shown in Figure 3 which were derived from searches for direct slepton (selectron and smuon) pair production and interpreted in the pMSSM. A similar dedicated analysis of the LEP data is required in order to *completely* rule out the light selectrons, and hence, the lightest neutralino DM mass below 30 GeV for the pMSSM scenario.

The neutralino DM-nucleon spin-independent scattering cross-sections for the allowed



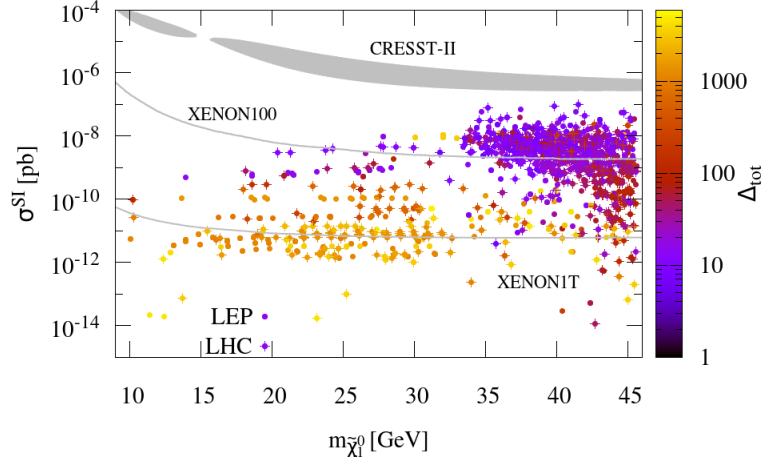


**Figure 2.** The gaugino ( $\tilde{B}$ ,  $\tilde{W}^0$ ) and higgsino ( $\tilde{H}_d^0$ ,  $\tilde{H}_u^0$ ) components of the lightest neutralino in our pMSSM parameter scan.



**Figure 3.** The various NLSP masses as a function of the LSP mass for the allowed points (circles) shown in Figure 1. The LEP exclusion regions strictly applicable for  $\tilde{\mu}_R$  (red shaded) and  $\tilde{\tau}_1$  (green shaded) and the LHC exclusion region for  $\tilde{\ell}$  ( $\ell = e, \mu$ ) (blue shaded) are also shown.

points is shown in Figure 4. It is interesting to note that most of the allowed region in Figure 1 with low fine-tuning lead to a higher scattering cross section via  $Z$ -boson exchange and are already ruled out by the latest XENON100 data [11]. The projected limit of XENON1T experiment [73] (and also LUX [74]) will be able to completely eliminate the low fine-tuning region for a light neutralino DM in pMSSM. In the light of the recent claims for positive hints of a light DM from some experiments, it is worth mentioning here that a few of our solutions with  $\sigma^{\text{SI}} \sim 10^{-7}$  pb are in the vicinity of the  $2\sigma$  preferred range of



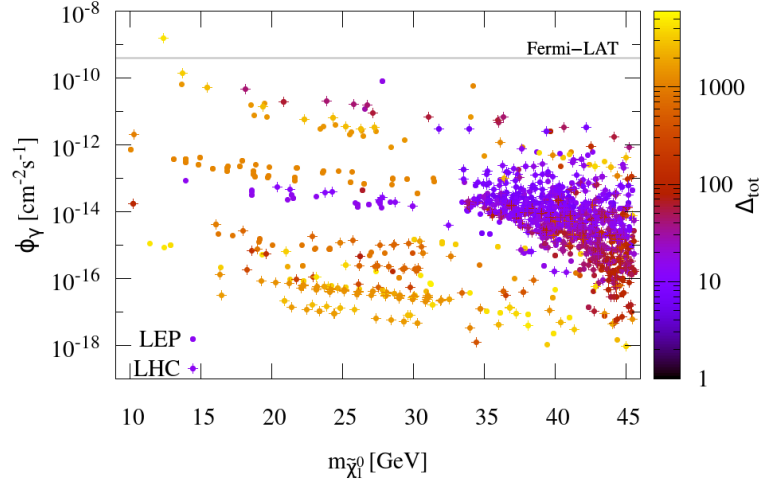
**Figure 4.** The spin-independent direct detection cross-section values for the allowed points in our pMSSM scan. The color-coding and labeling of the points are the same as in Figure 1. The current upper limit from the XENON100 experiment (upper solid line) and the projected limit from the XENON1T experiment (lower solid line) are shown as solid lines. The  $2\sigma$ -preferred range of CRESST-II is shown as the shaded region.

the CRESST-II results [10], but are ruled out by the XENON100 data.

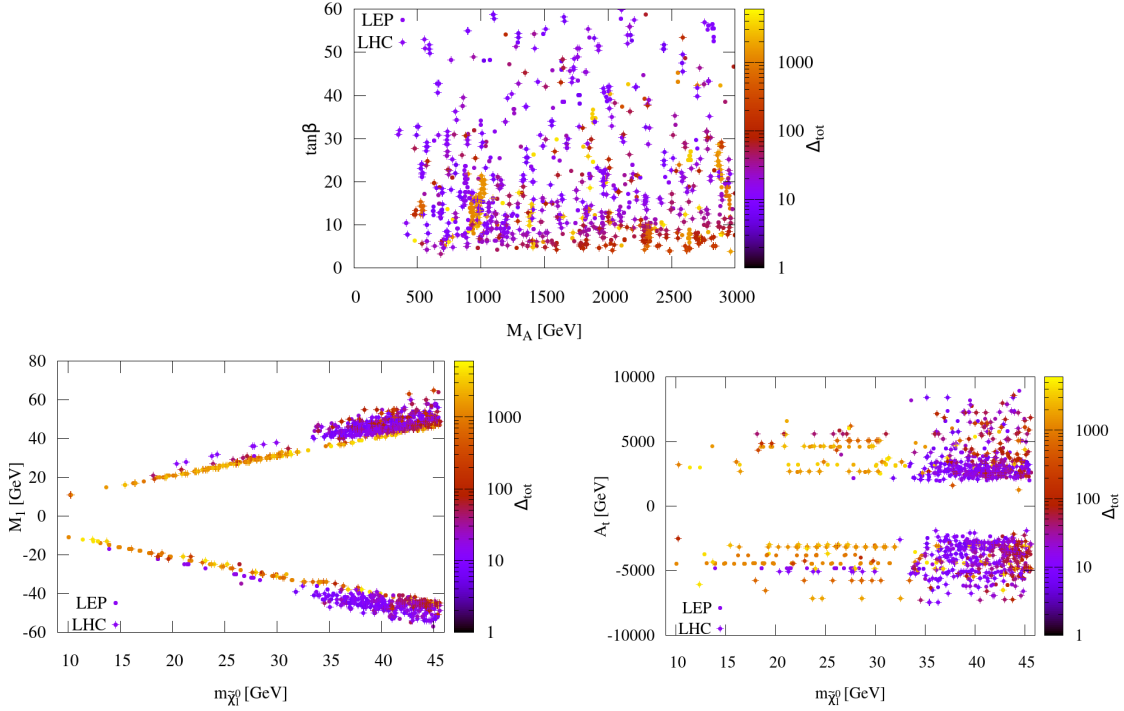
Figure 5 shows the integrated photon flux from the neutralino DM annihilation. Note that since the LSP in our case is mostly bino-like with heavy squarks and higgsinos and the charginos are not mass-degenerate with the LSP, the annihilation to photons is loop-suppressed, and hence, the photon line emission will be small. It is clear from Figure 5 that the current sensitivity of the Fermi-LAT [137] still leaves most of our allowed parameter space untouched. The future data from ongoing Fermi-LAT and next generation gamma-ray searches might be able to probe our allowed parameter space with a photon line signal [145].

For completeness, we also show in Figure 6 some other relevant pMSSM parameters with respect to the lightest neutralino mass. The  $m_A - \tan\beta$  parameter space is mostly consistent with the latest MSSM Higgs sector limits from the LHC [109, 110]. As for the bino mass parameter  $M_1$ , it is clear that a relatively small value of  $|M_1| < 100$  GeV is preferred to obtain a light bino-like neutralino LSP. Finally, as is well-known, a relatively large value of  $|A_t|$  is required in order to enhance the radiative corrections for the light  $CP$ -even Higgs mass to be consistent with the LHC-preferred value of  $125 \pm 2$  GeV.

Finally, we wish to point out that the allowed sparticle spectra discussed here with mostly heavy squarks, and with light sleptons, chargino and bino-like neutralino LSP, are also crucial for explaining the muon ( $g-2$ ) anomaly [146], while simultaneously satisfying all the other experimental constraints. Light staus with sizable left-right mixing can also lead to an enhanced  $h \rightarrow \gamma\gamma$  decay rate [147–149], which might be able to explain the persistent excess in the Higgs signal strength in this channel:  $1.65 \pm 0.24(\text{stat})^{+0.25}_{-0.18}(\text{syst})$  [150].



**Figure 5.** The integrated photon flux from annihilation of the neutralino DM as a function of its mass. The color-coding and labeling of the points are the same as in Figure 1. The solid horizontal line shows the current upper limit from the Fermi-LAT data.



**Figure 6.** The allowed parameter space for some of the relevant pMSSM parameters consistent with a light neutralino DM. The color-coding and labeling of the points are the same as in Figure 1.

## 5 Conclusion

We have studied the naturalness of a light neutralino dark matter candidate in the MSSM in the light of the latest results from the collider (LEP, Tevatron and LHC), flavor (LHCb) and dark matter (XENON100, WMAP-9, Planck) sectors. In particular, keeping in mind the

recent positive hints for a light DM below 45 GeV in some direct detection experiments and the null results from SUSY searches at the LHC, we perform a dedicated study focusing on the possibility of a light DM candidate in the form of the lightest neutralino in the pMSSM, also analyzing the naturalness of such a scenario. We include all the new results from the ongoing LHC experiments in our analysis, such as the null results from the SUSY searches, the observation of a Higgs-like particle, the observation of the rare meson decay  $B_s \rightarrow \mu^+ \mu^-$ , and the updated constraints on the MSSM Higgs sector. We also take into account the 9-year WMAP results as well as the recently released Planck results for the DM relic density and the Fermi-LAT data for the integrated photon flux. In order to efficiently scan over the 19-dimensional pMSSM parameter space, we perform a MCMC likelihood analysis optimized for a light neutralino with mass below the LEP bound of 46 GeV (applicable to gaugino mass unification models).

We find that a light neutralino DM with mass as low as 10 GeV is still allowed in the pMSSM, while satisfying all the existing experimental constraints. However, such neutralinos which are required to be mostly bino-like are severely fine-tuned and require the existence of light sleptons with mass below 100 GeV in order to provide an efficient annihilation channel to reduce the DM relic density below the observed upper limit. Such light smuons and staus are excluded from LEP searches while light selectrons are excluded only if we assume gaugino mass unification. A dedicated analysis of the LEP data in the context of a pMSSM scenario could completely eliminate the possibility of a light neutralino DM in the mass range of 10 - 30 GeV. We also find that for the allowed parameter space, other possible solutions in this mass range as discussed in the literature (e.g., light sbottom NLSP) are now excluded mainly due to the latest LHC results on the strongly interacting sfermion sector.

On the other hand, low fine-tuning regions can be obtained around  $m_{\tilde{\chi}_1^0} = 45$  GeV where the resonant annihilation via the  $s$ -channel  $Z$ -exchange is possible for a bino-higgsino mixture of neutralino LSP. However, such regions also predict a higher spin-independent DM-nucleon scattering cross section, and are mostly excluded by the recent XENON100 limits. The remaining such points are within the reach of the XENON1T projected limits.

In conclusion, while a light neutralino DM with mass below 46 GeV has been conclusively ruled out in MSSM with gaugino mass unification by LEP searches, such a possibility in a general version of MSSM is of enormous interest in the light of the recent claims for a positive signal in some DM direct detection experiments. Taking into account the latest experimental results from collider, flavor, dark matter and astrophysical/cosmological sectors, we show that such a light neutralino DM scenario is also getting highly constrained in MSSM without gaugino mass unification. However, within a pMSSM scenario, there still exists some parameter space for light neutralino DM which could be completely probed by a dedicated analysis of the existing experimental data, in combination with the ongoing searches.

## Acknowledgments

We thank Matthew Dolan and Patrick Janot for valuable discussions and comments on the draft, and Jonathan Da Silva for useful discussions regarding the MCMC analysis. CB is supported by the ERC advanced grant ‘DARK’ at IAP, Paris. The work of PSBD and AM is supported by the Lancaster-Manchester-Sheffield Consortium for Fundamental Physics under STFC grant ST/J000418/1. EP is supported by STFC ST/J501074.

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